# **CLAIM AMENDMENTS**

#### Claim Amendment Summary

### Claims pending

• Before this Amendment: Claims 1, 3-5, 7-37.

• After this Amendment: Claims 1, 3-5, 7-37

Non-Elected, Canceled, or Withdrawn claims: 2, 6

Amended claims: 1, 4-5, 9, 11, 13, 16-17, 20, 22, 28, 30, 35

New claims: None

#### Claims:

 (Currently Amended) A computer-readable <u>storage</u> medium having computer-executable instructions that, when executed, direct a computer to perform a method comprising:

obtaining a message M;

defining a vector v to be  $v_1,...,v_n$  based upon a predefined first hashing function of the message M:

calculating a private  $\ker \underline{\alpha} = \underline{\alpha}$  in accordance with this equation  $\alpha = \sum_{i=1}^n v_i \alpha_i \mod m$ , where m is an order of torsion points,  $\underline{\alpha}_i$  are scaling factors in  $\underline{O}_i$ 

### $= \alpha_i P$ $(1 \le i \le n)$ , and P and $Q_i$ are elliptical curve points;

producing a signature S in accordance with this equation:  $S = aH_2(M)$ ,  $S = aH_2(M)$ , where  $H_2(M)$  is a predefined second hashing function of the message M, wherein the predefined first hashing function differs from the predefined second hashing function and wherein the signature S is represented by a number of bits;

truncating a specific number of bits off of signature S;

after the truncating, indicating a message-and-signature pair (M, S) based, at least in part, on the obtaining, defining, calculating, or producing.

# 2. (Canceled)



- **3.** (**Original**) A medium as recited in claim 1, wherein the results of the indicating comprises a message-and-signature pair (M,  $\mu$ S) and the method further comprises calculating  $\mu = H_3(BK, M)$ , where BK is key and  $H_3(BK, M)$  maps M into an integer within a defined range.
- **4. (Currently Amended)** A medium as recited in claim 1, wherein the  $\alpha_i$ the  $\alpha_i$  are scaling factors for n discrete logs of  $\alpha_i P, ..., \alpha_n P$  base P, where n is a positive integer, P is a point on an elliptic curve and a public key.
- **5.** (Currently Amended) A medium as recited in claim 1, wherein  $\mathbf{e}_{r}$  are  $\underline{\alpha}_{i}$  are scaling factors for n discrete logs of  $\alpha_{1}P,...,\alpha_{n}P$  base P, where n is a positive integer, wherein P is a point on an elliptic curve;

a point P is of order m and where  $e_m(P,Q): E[m] \times E[m] \to GF(q)^*$  denotes a Tate or Weil or Squared Tate or Squared Weil Pairing, where  $\alpha_i P, ..., \alpha_n P = Q_1, ..., Q_n$  and where q is a prime power.

### 6. (Canceled)

- (Original) A medium as recited in claim 1, wherein the first hashing function produces values in {±1}.
  - **8. (Original)** A computing device comprising:

an output device:

a medium as recited in claim 1.

**9. (Currently Amended)** A computer-readable <u>storage</u> medium having computer-executable instructions that, when executed, direct a computer to perform a method <u>for</u> <u>facilitating enhanced security of a computing system</u> <u>without increasing a length of the short digital cipher, the method comprising:</u>

choosing n discrete logs of  $\alpha_1 P, ..., \alpha_n P$  base P, where n is a positive integer, P is a point on an elliptic curve and a public key, and a is a scaling factor and a private key;

indicating results of the choosing;

forging one or more short digital ciphers based upon the indicated results of the choosing, whereby the forging enhances security of a computing system without increasing a length of the short digital cipher.

- **10. (Original)** A medium as recited in claim 9, wherein a point P is of order m and where  $e_m(P,Q): E[m] \times E[m] \to GF(q)^*$  denotes a Tate or Weil or Squared Tate or Squared Weil Pairing, where  $\alpha_1 P, ..., \alpha_n P = Q_1, ..., Q_n$  and where q is a prime power.
- (Currently Amended) A medium as recited in claim 9 further comprising generating a digital signature based upon a message Mand-a, and α,.
  - **12. (Original)** A computing device comprising:

an output device;

a medium as recited in claim 9.



**13. (Currently Amended)** A method facilitating the production of a digital signature, the method comprising:

obtaining a message M;

defining a vector v to be  $v_1,...,v_n$  based upon a predefined first hashing function of the message;

calculating a private  $\frac{1}{key} = \alpha \ln \alpha$  accordance with this equation  $\alpha = \sum_{i=1}^{n} v_i \alpha_i \mod m$  where m is an order of torsion points, ,  $\alpha_i$  are scaling factors in

### $Q_i = \alpha_i P$ $(1 \le i \le n)$ , and P and $Q_i$ are elliptical curve points;

producing a signature S in accordance with this equation:  $S = aH_2(M)$ ,  $S = aH_2(M)$ , where  $H_2(M)$  is a predefined second hashing function of the message;

indicating results based, at least in part, on the obtaining, defining, calculating, or producing.

- **14. (Original)** A method as recited in claim 13 wherein the results of the indicating comprises a message-and-signature pair (*M, S*).
- **15. (Original)** A method as recited in claim 13, wherein the results of the indicating comprises a message-and-signature pair  $(M, \mu S)$  and the method further comprises calculating  $\mu = H_3(BK, M)$ , where BK is key and  $H_3(BK, M)$  maps M into an integer within a defined range.

- **16. (Currently Amended)** A method as recited in claim 13, wherein the  $\alpha_i$  the  $\alpha_j$  are scaling factors for n discrete logs of  $\alpha_i P, ..., \alpha_n P$  base P, where n is a positive integer, P is a point on an elliptic curve and a public key.
  - **17. (Currently Amended)** A method as recited in claim 13, wherein  $\mathbf{a}_r$  are  $\underline{\alpha}_i$  are scaling factors for n discrete logs of  $\alpha_i P, ..., \alpha_n P$  base P, where n is a positive integer, P is a point on an elliptic curve;

a point P is of order m and where  $e_m(P,Q): E[m] \times E[m] \to GF(q)^*$  denotes a Tate or Weil or Squared Tate or Squared Weil Pairing, where  $\alpha_1 P, ..., \alpha_n P = Q_1, ..., Q_n$  and where q is a prime power.

- **18.** (**Original**) A method as recited in claim 13, wherein the signature S is represented by a number of bits, wherein the method further comprises truncating a specific number of bits off of S before the indicating.
- **19.** (**Original**) A method as recited in claim 13, wherein the first hashing function produces values in  $\{\pm 1\}$ .

**20. (Currently Amended)** A computer-readable <u>storage</u> medium having computer-executable instructions that, when executed, direct a computer to perform a method comprising:

obtaining an input message-and-signature pair (M, S);

defining a vector v to be  $v_1,...,v_n$  based upon a predefined first hashing function of the message;

calculating a point Q on an elliptic curve in accordance with this equation:  $Q = \sum_{i=1}^n v_i Q_i$ ;

comparing pairing outputs of a pair (P, S) and a pair  $(Q, H_2(M))$ , where  $H_2(M)$  is a predefined second hashing function of M and P is a point on the elliptic curve;

indicating results of the comparing.

**21. (Original)** A medium as recited in claim 20 further comprising verifying the input message-and-signature pair (M, S) when the indicated results of the comparing is a match.

# 22. (Currently Amended) A medium as recited in claim 20, wherein:

the point P being a point on an elliptic curve and of order m and where  $e_m(P,Q): E[m] \times E[m] \to GF(q)^*$  denotes a Tate or Weil or Squared Tate or Squared Weil Pairing, where  $\alpha_1 P, \dots, \alpha_r P = Q_1, \dots, Q_r$  and where q is a prime power;

the  $\mathbf{a}_i$  the  $\mathbf{a}_i$  being scaling factors for n discrete logs of  $\alpha_i P, ..., \alpha_n P$  base P, where n is a positive integer.



**23. (Original)** A medium as recited in claim 20, wherein the method further comprises, when the indicated results of the comparing is not a match, modifying the vector  $\nu$  relative to its previous definition and repeating the defining, calculating, and comparing.

**24. (Original)** A medium as recited in claim 20, wherein the method further comprises:

when the indicated results of the comparing is not indicate a match, modifying the vector  $\nu$  relative to its previous definition;

repeating the defining, calculating, and comparing;

if the indicated results of the comparing still does not a match, then repeating the modifying and the repeating of the defining, calculating, and comparing until the indicated results do match.

**25. (Original)** A medium as recited in claim 20, wherein the method further comprises when the indicated results of the comparing is not a match, repeating the defining, calculating, and comparing with the defining being based upon a predefined third hashing function of the message.

**26. (Original)** A medium as recited in claim 20, wherein the signature *S* is represented by a number of bits, wherein the method further comprises padding *S* with a specific number of bits before the defining.

27. (Original) A computing device comprising:

an output device;

a medium as recited in claim 20.

**28. (Currently Amended)** A method facilitating the verification of a digital short-signature, the method comprising:

obtaining, by a short-signature verifier configured to verify a valid digital short signature, an input message-and-signature pair (*M*, *S*);

defining, by the short-signature verifier, a vector  $\nu$  to be  $\nu_1,...,\nu_n$  based upon a predefined first hashing function of the message;

calculating, by the short-signature verifier, a point Q on an elliptic curve in accordance with this equation:  $Q = \sum_{i=1}^n v_i Q_i$ ;

comparing, by the short-signature verifier, pairing outputs of a pair (P, S) and a pair  $(Q, H_2(M))$ , where  $H_2(M)$  is a predefined second hashing function of M and P is a point on the elliptic curve;

indicating, by the short-signature verifier, results of the comparing .

**29. (Original)** A method as recited in claim 28 further comprising verifying the input message-and-signature pair (*M, S*) when the indicated results of the comparing is a match.

**30.** (Currently Amended) A method as recited in claim 28, wherein

the point P being a point on an elliptic curve and of order m and where  $e_m(P,Q): E[m] \times E[m] \to GF(q)^*$  denotes a Tate or Weil or Squared Tate or Squared Weil Pairing, where  $\alpha_i P, ..., \alpha_i P = Q_i, ..., Q_r$  and where q is a prime power;

the  $a_i$ the  $a_i$  being scaling factors for n discrete logs of  $\alpha_i P, ..., \alpha_n P$  base P, where n is a positive integer.

**31. (Original)** A method as recited in claim 28 further comprising, when the indicated results of the comparing is not a match, modifying the vector  $\nu$  relative to its previous definition and repeating the defining, calculating, and comparing.

**32. (Original)** A method as recited in claim 28 further comprising:

when the indicated results of the comparing is not a match, modifying the vector  $\nu$  relative to its previous definition;

repeating the defining, calculating, and comparing;

if the indicated results of the comparing still does not a match, then repeating the modifying and the repeating of the defining, calculating, and comparing until the indicated results do match.

**33. (Original)** A method as recited in claim 28 further comprising when the indicated results of the comparing is not a match, repeating the defining, calculating, and comparing with the defining being based upon a predefined third hashing function of the message.

**34. (Original)** A method as recited in claim 28, wherein the signature *S* is represented by a number of bits, wherein the method further comprises padding *S* with a specific number of bits before the defining.

**35. (Currently Amended)** A computer-readable <u>storage</u> medium having computer-executable instructions that, when executed , direct a computer to perform a method comprising:

obtaining an input message-and-signature pair (M, S');

defining a vector v to be  $v_1,...,v_n$  based upon a predefined first hashing function of the message;

calculating a point Q on an elliptic curve in accordance with this equation:  $Q=\sum_{i=1}^n v_iQ_i$ ;

comparing pairing outputs of a pair (P, S) and a pair  $(Q, H_2(M))^{\mu}$ , where  $H_2(M)$  is a predefined second hashing function of M and P is a point on the elliptic curve and  $\mu$  is an integer in a defined range;

indicating results of the comparing.

**36. (Original)** A medium as recited in claim 35 further comprising verifying the input message-and-signature pair (M, S) when the indicated results of the comparing is a match.

**37.** (Original) A computing device comprising:

an output device;

a medium as recited in claim 35.